

Automatic Control, Basic Course

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Dept. of Automatic Control at Lund University



- ▶ Founded in 1965 by Karl Johan Åström
- ▶ Approx. 50 persons
- ▶ M-building floors 1,2,5

Goal of the Course

The aim of the course is to give knowledge about the **basic principles of feedback control**.

The course will give insight into what can be achieved with control—the possibilities and limitations.

The course focuses on **linear continuous-time systems**.

Like More Control Theory?

Follow the parallel course

[Control Theory 3hp](#)

First Lecture: Thursday 20/1 at 8.15-10, M:D

Bo Bernhardsson

Academia

- ▶ LTH - E81, MSc 1986
- ▶ PhD in Automatic Control, Lund University, 1992.
- ▶ Post-doc at Univ. of Minnesota 1992-93
- ▶ Associate Professor etc, Lund University, 1993-1999
- ▶ Professor 1999-2001, on leave 2001-2010

Industry

- ▶ Senior Researcher/Specialist, Ericsson, Lund 2001-05
- ▶ Expert, Ericsson 2005-2010 (80/20 split with LU)
- ▶ Expert area: "Mobile System Design and Optimization"
- ▶ 15 granted patents in the area of mobile communications
- ▶ 10⁹ control loops

Course Program

15 Lectures

15 Exercises

3 Mandatory Laborations, sign up for lab1 asap

Literature

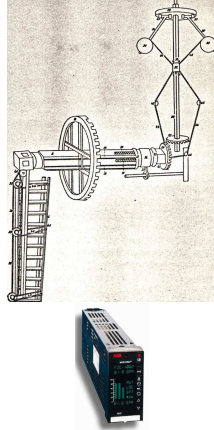
Exam

Introduction to Control

Switch to other presentation

The PID Controller

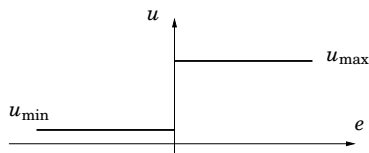
- ▶ The oldest controller type
- ▶ The most widely used
 - ▶ Pulp & paper industry 86%
 - ▶ Steel industry 93%
 - ▶ Oil refineries 93%



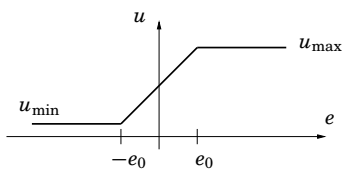
On/Off Control

Control error: $e = r - y$

$$u = \begin{cases} u_{\min}, & e < 0 \\ u_{\max}, & e > 0 \end{cases}$$



Proportional Control



$$u = \begin{cases} u_{\max}, & e > e_0 \\ u_0 + Ke, & -e_0 < e < e_0 \\ u_{\min}, & e < -e_0 \end{cases}$$

K – proportional gain

u_0 – bias term (often 0)

Stationary Error with P Control

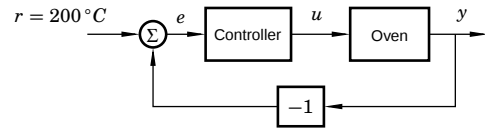
Assume the controller works within the proportional band ($-e_0 < e < e_0$). Then

$$e = \frac{u - u_0}{K}$$

Two ways to reduce the stationary control error:

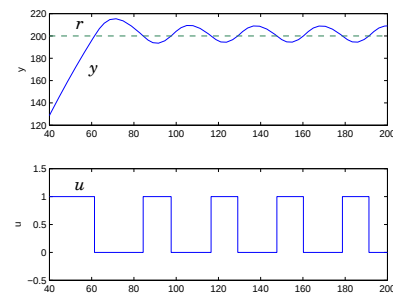
- ▶ Make K larger
- ▶ Adjust u_0

Example: Oven



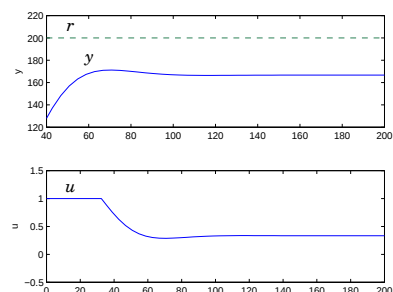
- ▶ y – actual temperature
- ▶ r – desired temperature
- ▶ e – control error
- ▶ u – heating element power ($0 \leq u \leq 1$)

On/Off Control – Oven Example



- ▶ Oscillations

P Control – Oven Example

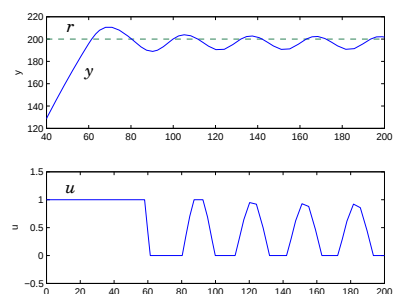


- ▶ Stationary error

(What is the value of K in the simulation above, $u_0 = 0$?)

P Control – Oven Example

Increased gain K :



- ▶ Smaller stationary error
- ▶ Larger oscillations

Proportional–Integral Control

Add automatic adjustment of the bias term (“automatic reset”)
Keep adjusting the control signal as long as there is an error

PI-controller:

$$\begin{aligned} u(t) &= K e(t) + K_i \int_0^t e(s) ds \\ &= K \left(e(t) + \frac{1}{T_i} \int_0^t e(s) ds \right) \end{aligned}$$

T_i – integral time

The Amazing Property of Integral Action

Consider a PI-controller:

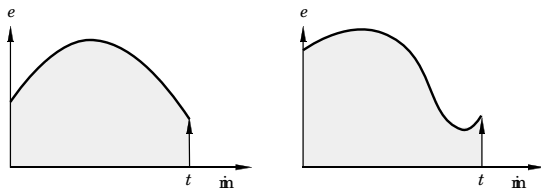
$$u(t) = K e(t) + K_i \int_0^t e(s) ds$$

Assume that there is an equilibrium with constant $e(t) = e_0$ and $u(t) = u_0$. Then we must have $e_0 = 0$!

Can you explain this?

Limitations of PI Control

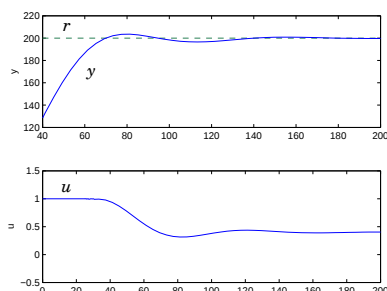
A PI controller gives the same control signal in these two cases:



Problematic for processes with inertia, e.g.

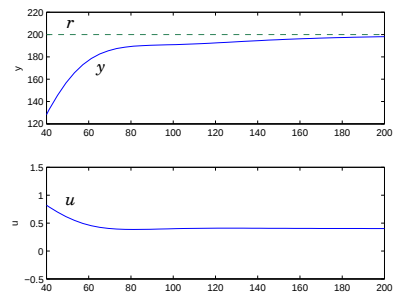
- ▶ temperature
- ▶ position

PID Control – Oven Example



- ▶ Reduced oscillations

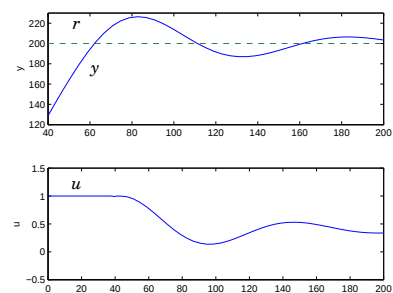
PI Control – Oven Example



- ▶ No stationary error

PI Control

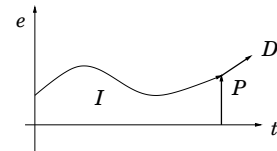
Smaller integral time T_i (i.e. larger integral action):



- ▶ Larger oscillations

PID Control

Add prediction of the control error



PID-controller:

$$u(t) = K \left(e(t) + \frac{1}{T_i} \int_0^t e(s) ds + T_d \frac{de(t)}{dt} \right)$$

T_d – derivative time

Laboratory Exercise 1



Control of the water level in the upper or lower tank

- ▶ Open-loop and closed-loop control
- ▶ Manual and automatic control
- ▶ Empirical tuning of P, PI and PID controllers

Laborations - Lab 1

The manuals for Labs 2 and 3 contain **preparatory assignments** that must be solved before the laboratory exercise.

At the start of Lab 2, a **quiz** with two review questions will also be given. You must give correct answers to both questions in order to proceed with the laboratory exercise.

Signup for Lab 1 at home page now.

No written lab reports.

What You Should Do Now

- ▶ Sign up for Lab1 asap !
- ▶ Read course program and get all material
- ▶ Read math repetition material if needed
- ▶ Read first lecture in [TH]