

## Session 4

*Realizations from weighting patterns, impulse responses, and Markov parameters. Minimal Realizations*

### Reading Assignment

Rugh Ch 10, 11 (only pp194-199, skip proof of 11.7), (26: skip all proofs, scan definitions, examples and theorems, max 30min)

**Exercise 4.1** = Rugh 10.2

**Exercise 4.2** = Rugh 10.7

**Exercise 4.3** = Rugh 10.9

**Exercise 4.4** = Rugh 10.12

**Exercise 4.5** = Rugh 26.5

**Exercise 4.6** = Rugh 11.12

**Exercise 4.7** Perform the calculations in Rugh Example 26.21 (p497) for  $\alpha = -2, 0, 1$ .

**Exercise 4.8** = Rugh 26.7

### Hand in problems

**Exercise 4.9** The following system is given

$$\begin{aligned} \dot{x}_1 &= \sin(t)u(t) \\ \dot{x}_2 &= \cos(t)u(t) \\ y(t) &= \sin(t)x_1(t) + \cos(t)x_2(t) \end{aligned}$$

Calculate the weighting pattern, and show that it is stationary. Then give a time invariant realisation.

**Exercise 4.10** Find a minimal realization of

$$G(s) = \begin{bmatrix} \frac{s+1}{s^2+2s+1} & \frac{s}{s^2+1} \\ \frac{1}{s+2} & \frac{2}{s^2+3s+2} \end{bmatrix}$$